

# ASSIGNMENT 4

## ECON 6501: URBAN AND REGIONAL ECONOMICS

Due **Thursday, 28 May, 6:00pm**. Students are welcome to discuss homework in groups, but each student must prepare and submit a unique assignment. Note the names of other group members. All assignments must be neat and professional. Answer all parts of all questions, or include a copy of your midterm exam as a substitute for questions that received full credit.

1. Consider a monocentric city model where residents all work at  $x = 0$ . A fixed number of residents,  $H$ , live in the city. The boundary between residential and agriculture land is governed by a green belt law, which outlaws resident living more than  $B$  distance from the city center. Residents can buy land ( $q$ ) for the location dependent rate  $p(x)$  and purchase nonland consumption ( $c$ ) for price 1. Residents pay a monetary commuting  $tx$ , so at location  $x$  the consumer's budget constraint is  $pq + c + tx = y$ . (The income level  $y$  is sufficiently large that non-negativity constraints are not binding.) Residents have identical preferences given by

$$u(c, q) = c \cdot q - \beta B.$$

- (a) Find the price of land,  $p$ , as a function of  $x$ ,  $H$ , and  $B$ .
- (b) Find the utility level residents can attain as a function of  $B$ .
- (c) Find the green belt distance  $B$  that would maximize the welfare of residents.